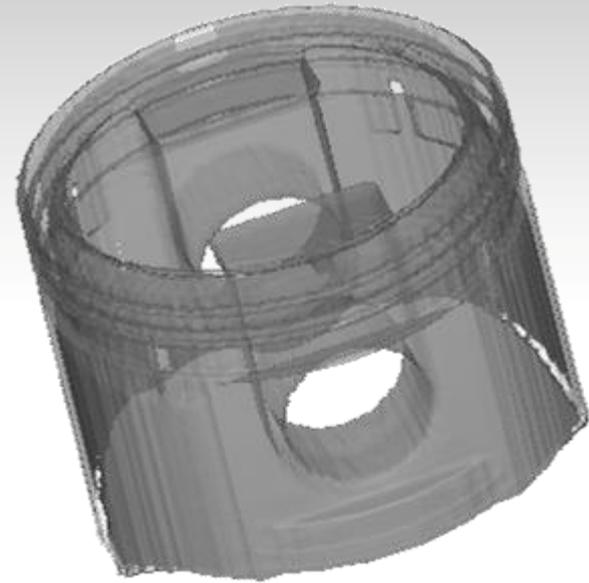
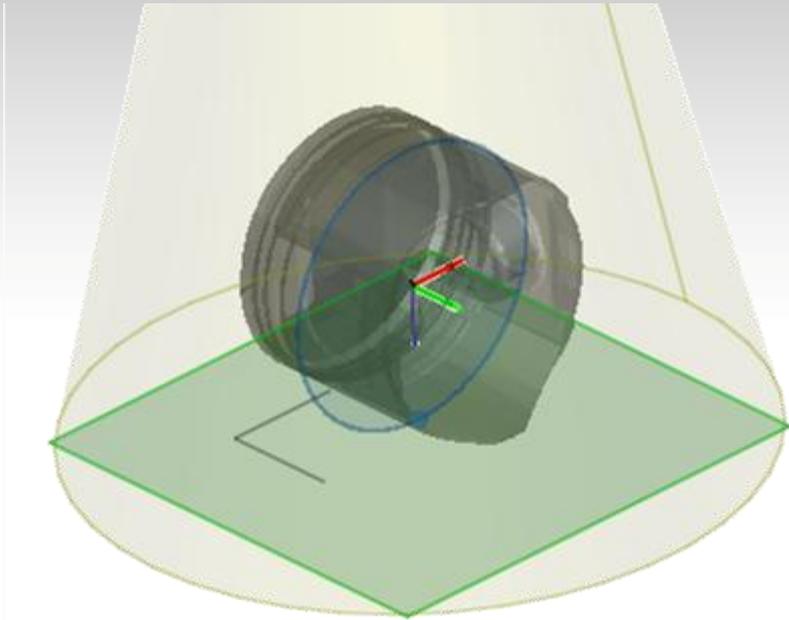


# CIVA Computed Tomography Modeling



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**CIVA**

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energie atomique • energies alternatives

18<sup>th</sup> WCNT, 16-20 April 2012, Durban, South Africa

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# Summary

- | Context
- | From CIVA RT to CIVA CT
- | Reconstruction Methods
- | Applications
  - Example of Source/detector misalignment
  - Comparison study

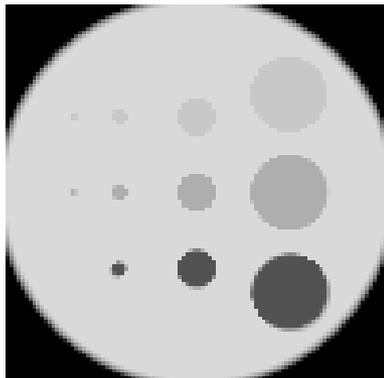
# Context



- | Computed Tomography (CT) is becoming a standard tool in many domains:
  - Material Structure, Earth science, archeology
  - Medical imaging...
- | In NDT, tomography is mostly used to provide internal information such as:
  - Inclusions, Cracks, Porosities,
  - Characteristics of the internal structure...
- | Experimental CT is a relatively complex process
- | Simulation allows to:
  - Test and evaluate the performances of an experimental CT system
  - Optimize the performance by a correct choice of parameters

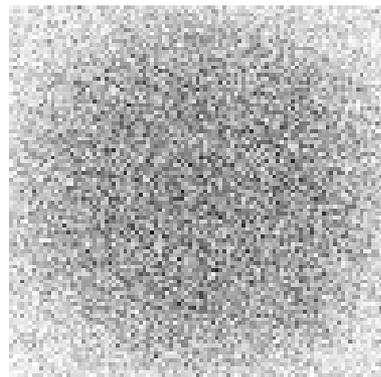
# From CIVA RT to CIVA CT

- | Simulation studies of radiographic inspections with CIVA (since 2007)
  - Simulation of complex parts
  - Direct and scattered radiation
  - Gamma and X sources

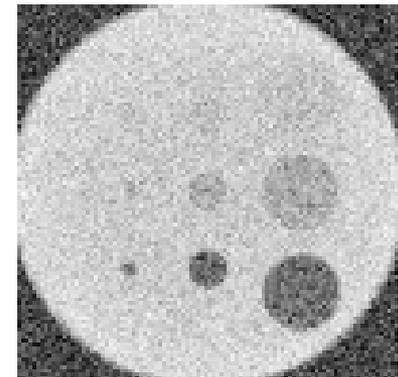


Direct radiation

+



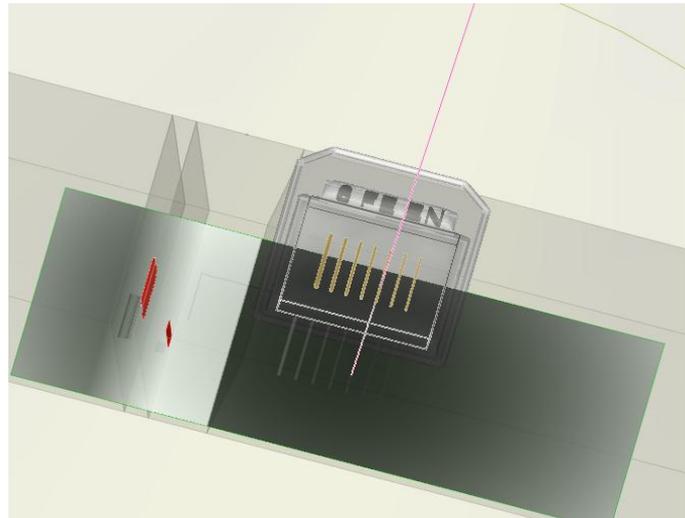
Scattered radiation



Final image

# From CIVA RT to CIVA CT

- | Simulation studies of radiographic inspections with CIVA (since 2007)
  - Different types of detectors
  - Influential parameters accounting for
  - IQI available

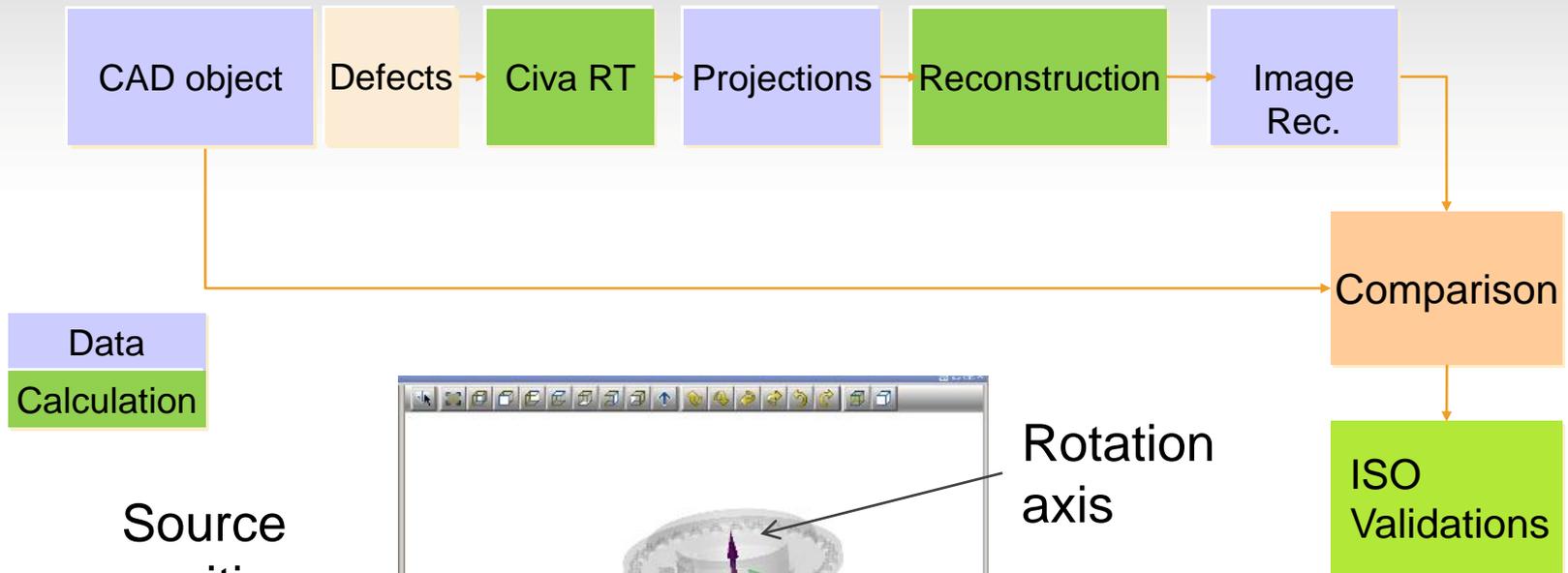


# Parameters in CT

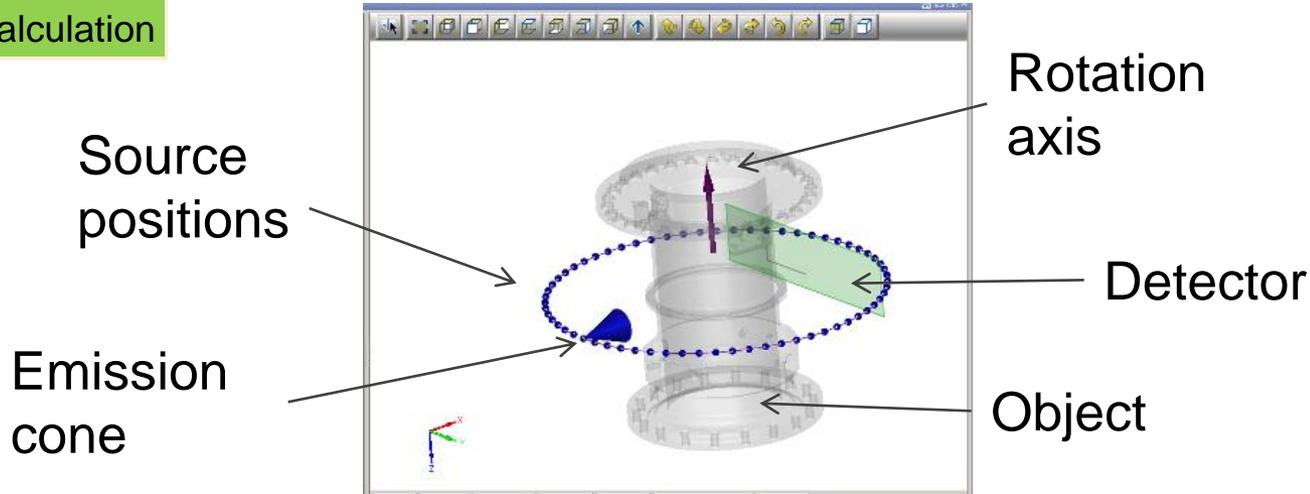
- | « Radiology » parameters
  - Geometry
  - Spectra, intensity, exposure time
  - Filters
  - Processing (for digital radiology)
  
- | Specific « CT » parameters
  - Projections angles/positions
  - Number of projections
  - Reconstruction algorithms
  - Post processing

# From CIVA RT to CIVA CT

## | New Computed Tomography module in CIVA

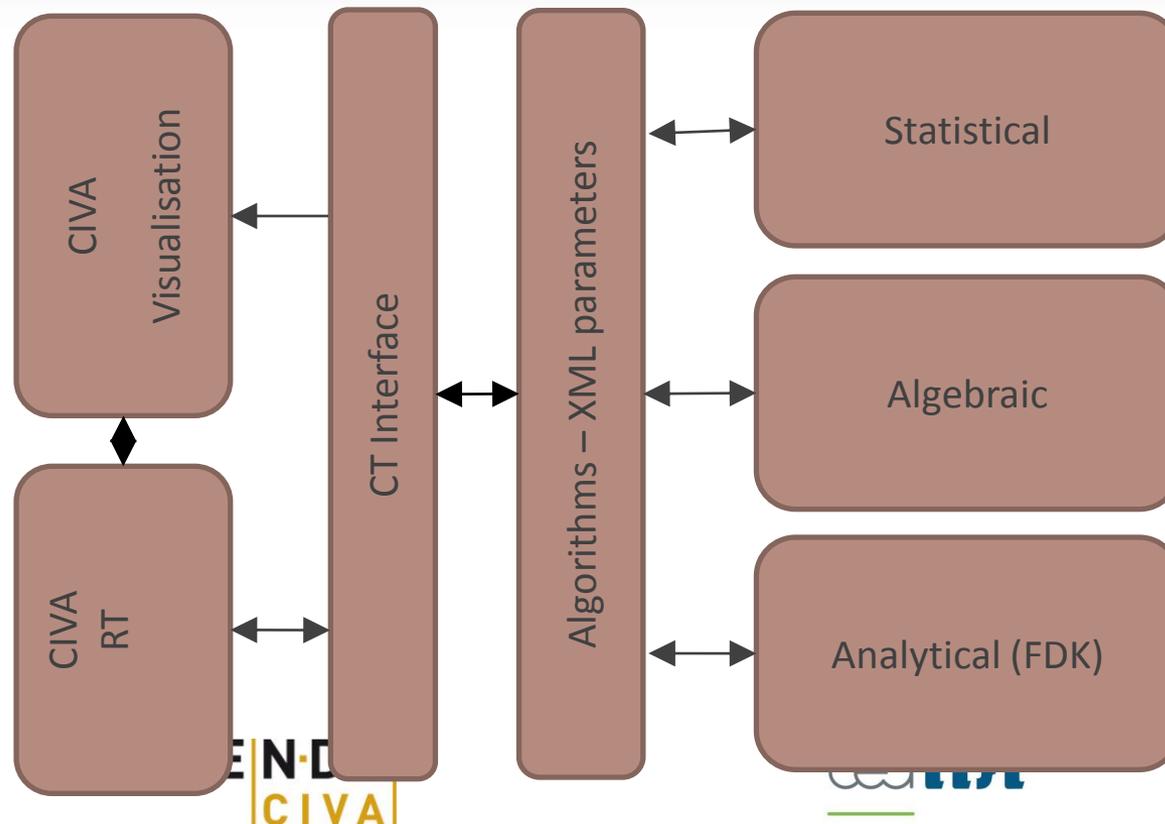


Data  
Calculation



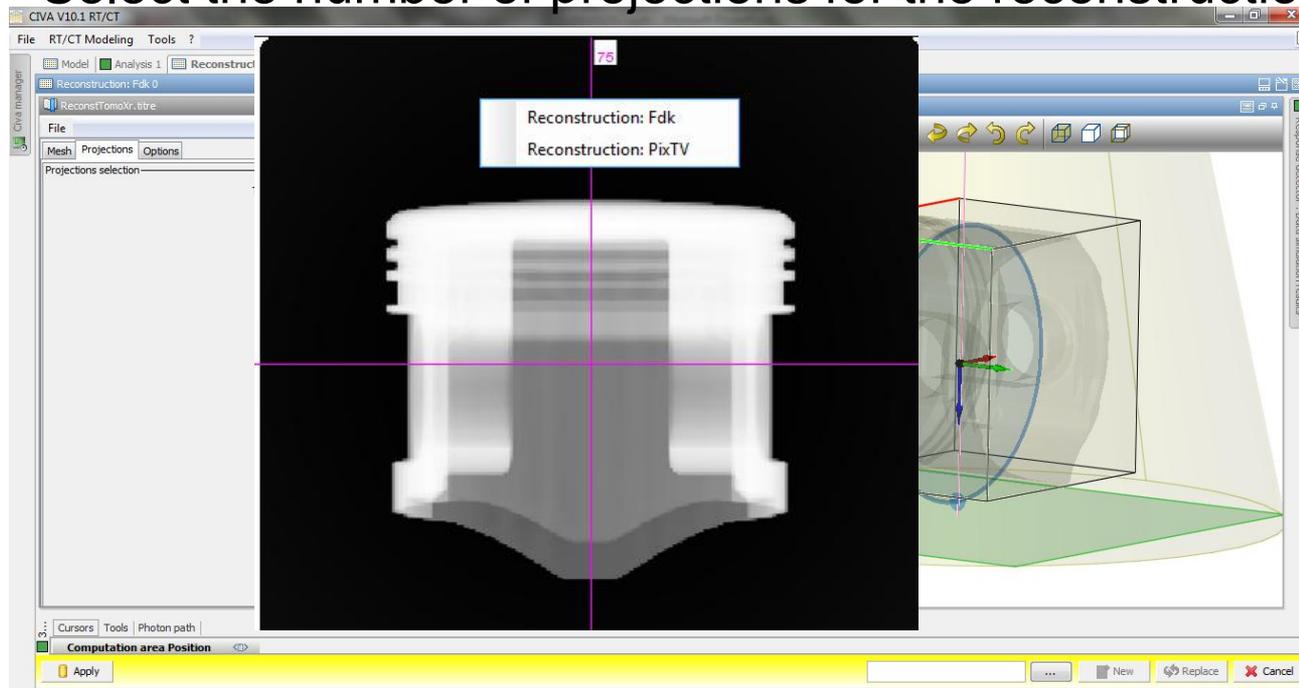
# From CIVA RT to CIVA CT

- Several CT reconstruction algorithms are implemented as plugins:
  - possibility to implement various algorithms on different hardware
  - Possibility to compare the different algorithms



# Reconstruction methods

- | Two algorithms available in the current version :
  - FDK
  - PIXTV
- | Possibility to:
  - Define the reconstruction zone
  - Select the number of projections for the reconstruction



# Reconstruction with FDK algorithm



I FDK (Feldkamp-Davis-Kress) algorithm is a 3D analytic reconstruction method:

- Reconstructs the function  $f(x,y,z)$ , which is a map of the linear attenuation coefficients of the imaged sample
- It is a three step algorithm of the filtered back-projection type (FBP) for cone-beam data:

- Weighting: 
$$R'_\beta(p, \zeta) = \frac{D_{SO}}{\sqrt{D_{SO}^2 + \zeta^2 + p^2}} R_\beta(p, \zeta)$$

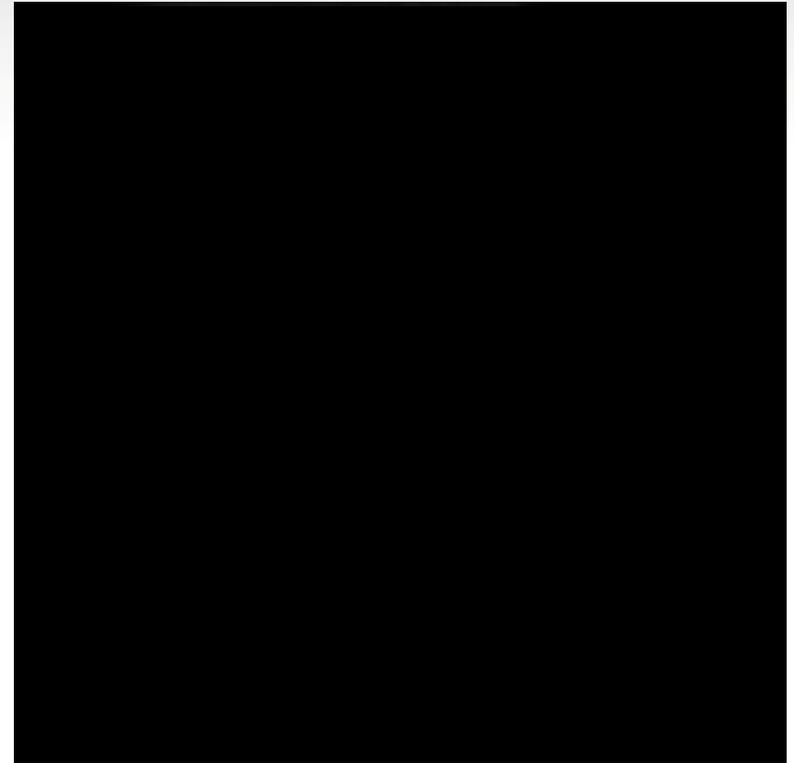
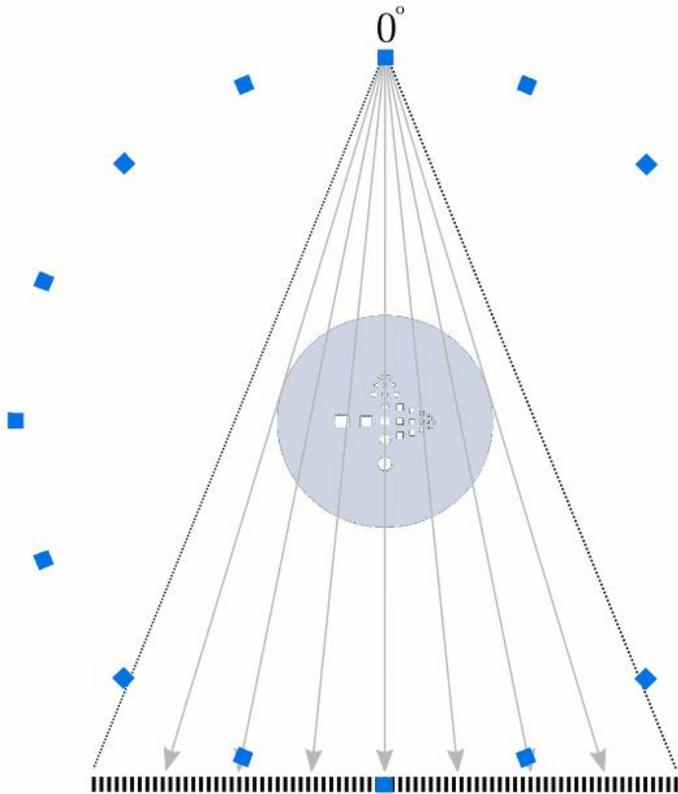
- Filtering (convolution): 
$$Q_\beta(p, \zeta) = R'_\beta(p, \zeta) * g(p)$$

- Backprojection: 
$$f(x, y, z) = \int_0^{2\pi} \frac{1}{U^2} Q_\beta\left(\frac{x \cos(\beta) + y \sin(\beta)}{U}, \frac{z}{U}\right) d\beta$$

where: 
$$U = \frac{D_{SO} + x \sin(\beta) - y \cos(\beta)}{D_{SO}}$$

# Reconstruction with FDK algorithm

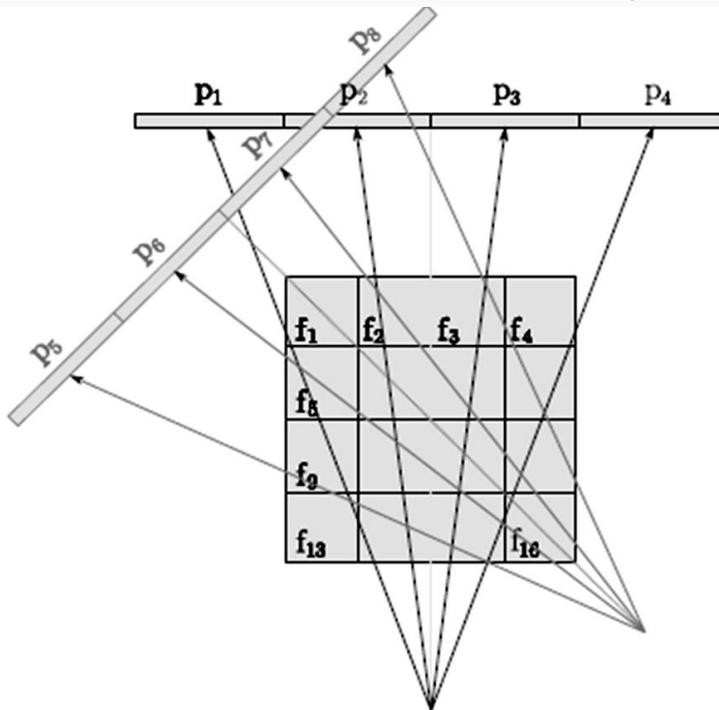
$$\mu \mapsto f(x, y, z)$$



CT image

# Reconstruction with PIXTV algorithm

- PixTV is an iterative reconstruction algorithm which minimizes the TV (total variation) norm:
  - Uses the linear data model for the CT problem
  - Projection and image space discretized and represented as a



$$p_k = \sum_{l=0}^N a_{k,l} \cdot f_l$$

- $p_k$  is a vector containing the projection data for a ray  $k$ ,
- $N = n^2$  is the total number of pixels,
- $a$  is the system matrix,
- $f$  is the image to be reconstructed (reshaped as a vector containing the attenuation values)

# Reconstruction with PIXTV algorithm



- Reconstruction → solving a convex optimization problem

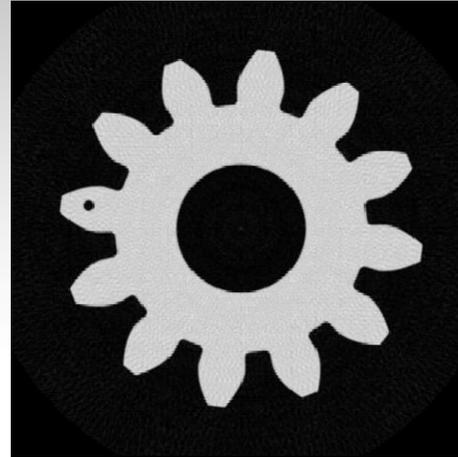
$$\min_f \frac{\mu}{2} \|Af - p\|^2 + \|f\|_{TV}, s.t. f \in C$$

- where  $\mu$  is a penalty coefficient,
  - A represents the system matrix,
  - f the CT image, p the projection data (sinogram)
  - C a constraint set of possible solutions.
- 
- TV (total variation) regularization

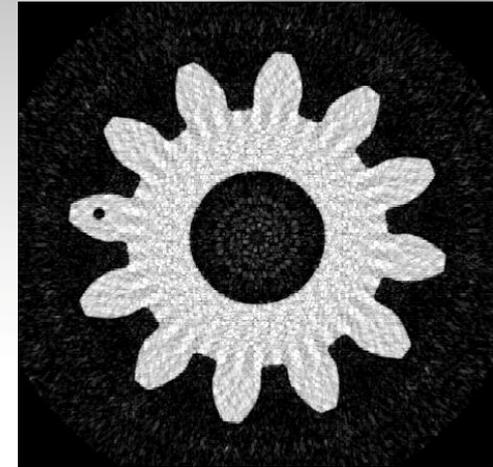
# Comparaison FDK vs PIXTV

## | FDK

- Analytic algorithm: fast
- Implemented on CPU (multithread)
- An important number of projections is needed
- Robust



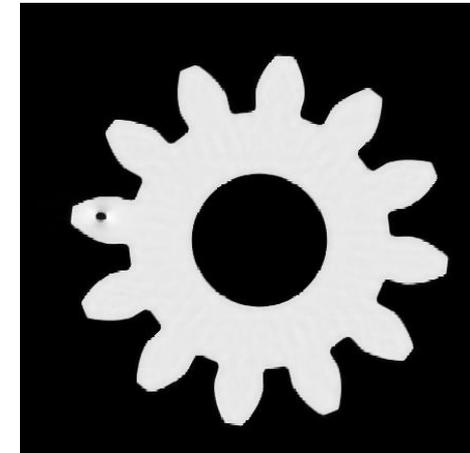
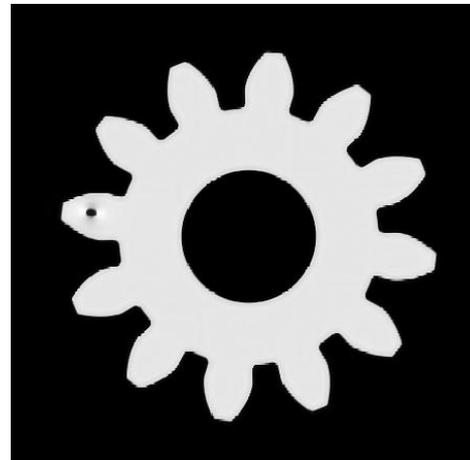
360 projections



90 projections

## | PIX TV

- Iterative algorithm: slower
- Implemented on GPU
- Less projections are needed
- Many parameters
- Difficult parameter choice ( $\mu$ )



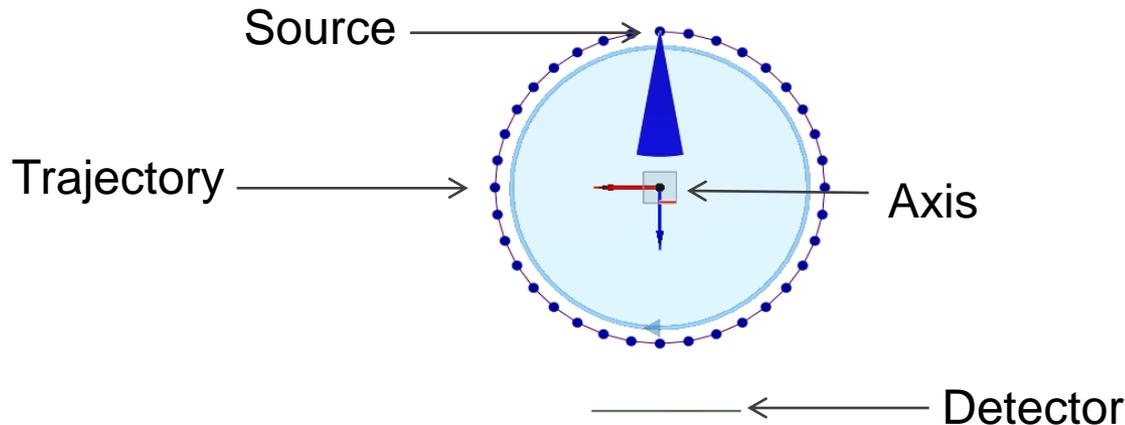
# Applications:

## Example of Source/detector misalignment

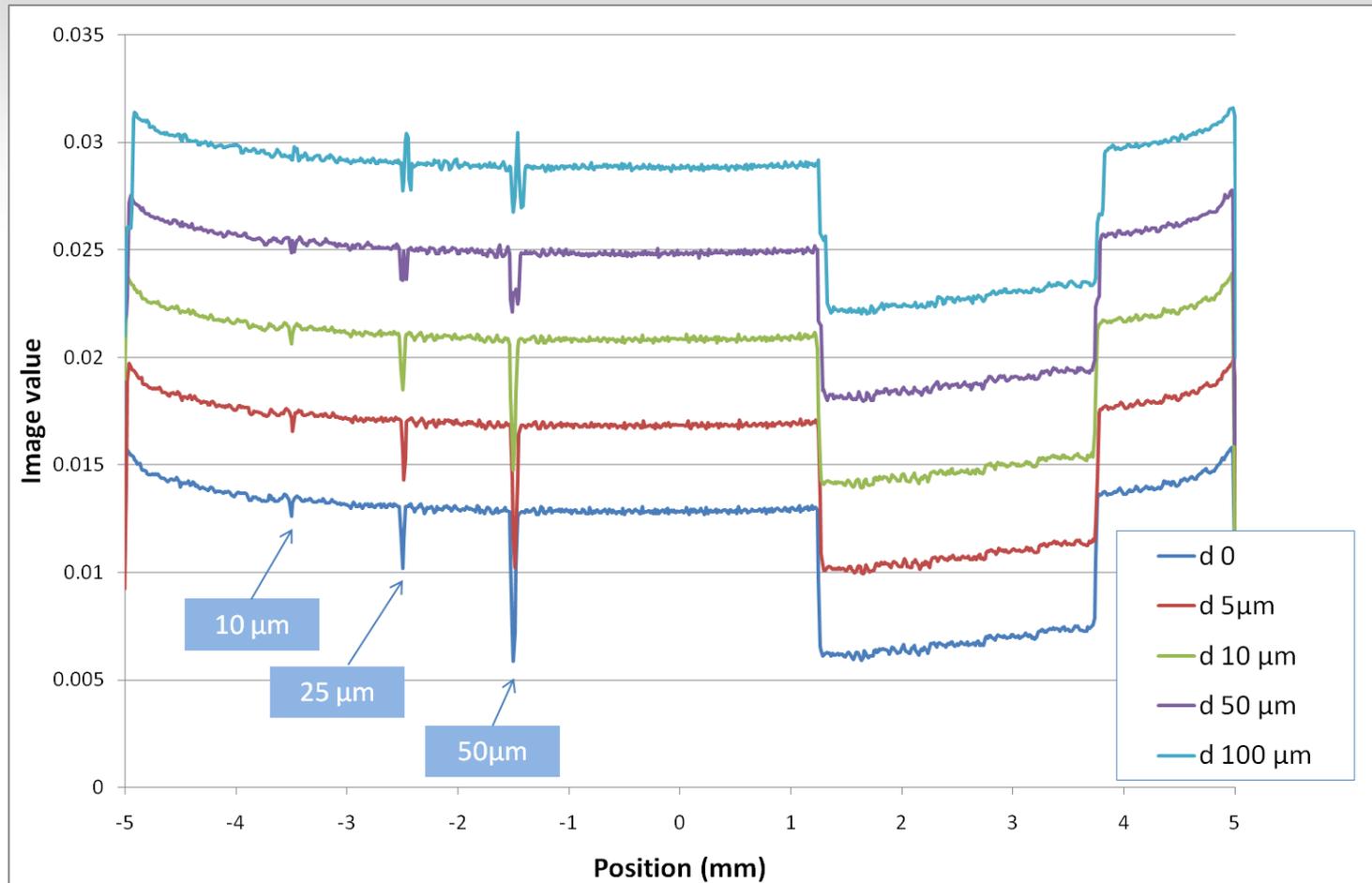
- | Estimate the influence of the rotation axis mispositioning
  - Detector:
    - CsI X-ray detector
    - Thickness 300 $\mu$ m ; 1024 x 128 pixels ; 50 $\mu$ m/pixel
  - Source to object distance : 50mm
  - Source to detector distance : 200mm
  - Object :
    - Aluminum cylinder of 10mm in diameter
    - Two sets of aligned holes of diameter 5, 10, 25, 50 $\mu$ m and 50,100, 250 and 500 $\mu$ m and 5 stacked carbon blocks
  - 90kV X-ray generator

# Applications: source/detector misalignment

- | Estimate the influence of the rotation axis mispositioning
  - 360 projections (for all simulations)
  - Images are reconstructed with FDK.
  - The rotation axis shifted perpendicularly in the horizontal plane with 5, 10, 50 and 100 $\mu$ m



# Applications: source/detector misalignment

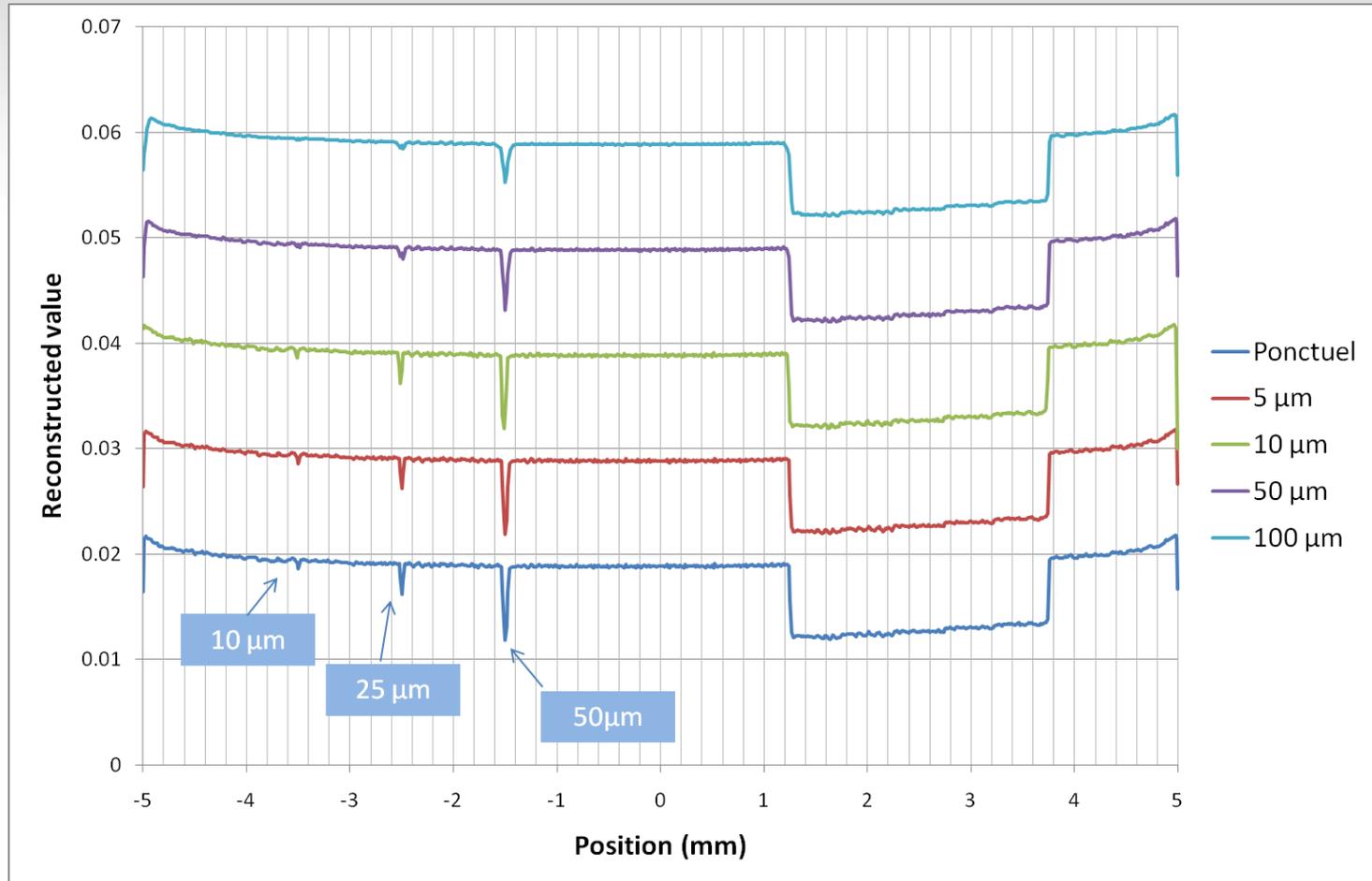


# Applications: Spot size influence



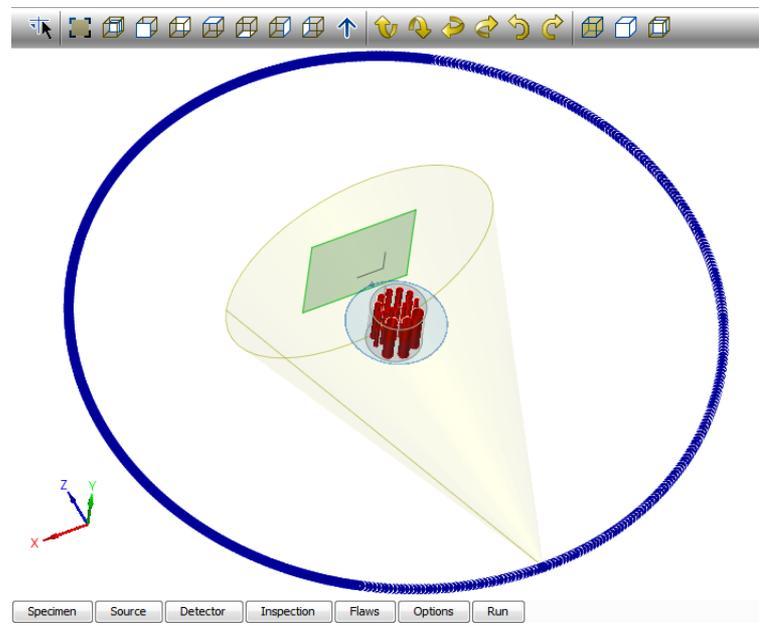
- | Evaluate the influence of the X-ray spot size in a micro-CT configuration
  - Same nominal configuration as the previous one
  - X-ray spot size has been set to 0, 5, 10, 50 and 200 $\mu$ m

# Applications: Spot size influence



# Applications: comparison study

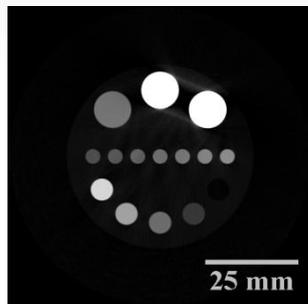
- | Evaluate the performance of the presented reconstruction algorithms
  - The X-ray source is a reflection type X-ray generator
  - Acceleration voltage of 100kV
  - Target current of 10mA
  - The sample is a Plexiglas cylinder of 50mm in diameter
  - 15 cylindrical insertions of different materials and densities



# Applications: comparison study

- Performance of the reconstruction algorithms
  - Simulation of 512 projections equally distributed over a full rotation
  - Reconstructions of the central plane from the complete set of projections.

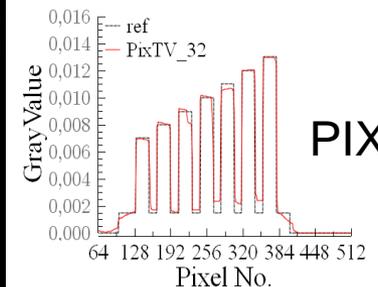
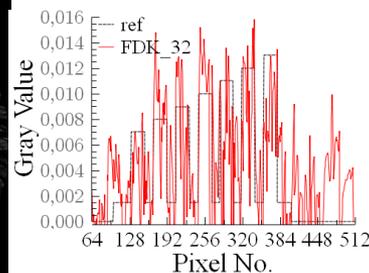
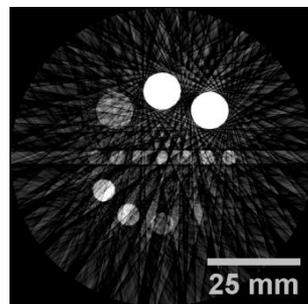
FDK



PIXTV

- evaluation for the cases of reconstruction from a lower number of projections: 32 equi-distributed projections

FDK



PIXTV

# Conclusion and future works



## Full modeling of Computed Tomography in CIVA for:

- Performances estimations
- Optimization of control parameters
- Benchmark of reconstruction algorithms with realistic data

## Future works:

- Import and reconstruct experimental data
- Integrate quantitative criteria to enhance benchmarking
- POD module
- Accelerating Monte Carlo computation (scattering photons)
- Development of a specific image processing module
- Implementation of new reconstruction algorithms